

Applied Maths Induction Workshop 2 – Relative Motion – Exercises

2009 – Ordinary Level – Question 2

A ship P is moving north at a constant speed of 20 km/h.

Another ship Q is moving south-west with a constant speed of $10\sqrt{2}$ km/h.

At a certain instant, P is positioned 50 km due west of Q.



- (ii) the velocity of Q in terms of \vec{i} and \vec{j} .
- (iii) the velocity of *P* relative to *Q* in terms of \vec{i} and \vec{j} .
- (iv) the shortest distance between P and Q in the subsequent motion.

2006 – Ordinary Level – Question 2

Ship *A* is travelling east α° north with a constant speed of 39 km/h, where $\tan \alpha = \frac{5}{12}$. Ship *B* is travelling due east with a constant speed of 16 km/h. $B \xrightarrow{16 \text{ km/h}} 39 \text{ km/h}$

At 2pm ship B is positioned 90 km due north of ship A.

- (i) Express the velocity of ship A and the velocity of ship B in terms of \vec{i} and \vec{j} .
- (ii) Find the velocity of ship A relative to ship B in terms of \vec{i} and \vec{j} .
- (iii) Find the shortest distance between the ships.



2004 – Higher Level – Question 2(b)

At time t = 0, two particles P and Q are set in motion.

At time t = 0, Q has position vector $20\vec{i} + 40\vec{j}$ metres relative to P.

P has a constant velocity of $3\vec{i} + 5\vec{j}$ m/s and *Q* has a constant velocity of $4\vec{i} - 3\vec{j}$ m/s.

Find

- (i) the velocity of Q relative to P
- (ii) the shortest distance between P and Q, to the nearest metre
- (iii) the time when P and Q are closest together, correct to one decimal place.

1996 – Higher Level – Question 2

A ship *B*, is travelling due West at $25 \cdot 6 \text{ km/h}$. A second ship, *C*, travelling at 32 km/h is first sighted 17 km due north of *B*. From *B* the ship *C* appears to be moving South-east.

Find

- (i) the direction in which C is actually moving
- (ii) the velocity of C relative to B
- (iii) the shortest distance between the ships in the subsequent motion
- (iv) the time that elapses, after first sighting, before the ships are again 17 km apart.

2007 – Higher Level – Question 2(a)

Ship *B* is travelling west at 24 km/h. Ship *A* is travelling north at 32 km/h. At a certain instant ship *B* is 8 km north-east of ship *A*.

- (i) Find the velocity of ship A relative to ship B.
- (ii) Calculate the length of time, to the nearest minute, for which the ships are less than or equal to 8 km apart.

2002 – Higher Level – Question 2(a)

Two boats, *B* and *C*, are each moving with constant velocity. At a certain instant, boat *B* is 10 km due west of boat *C*. The speed and direction of boat *B* relative to boat *C* is $2 \cdot 5 \text{ m/s}$ in the direction 60° south of east.

- (i) Calculate the shortest distance between the two boats, to the nearest metre.
- (ii) Calculate the length of time, to the nearest second, for which the boats are less than or equal to 9 km apart.

2009 – Higher Level – Question 2(a)

Two cars, A and B, travel along two straight roads which intersect at right angles.

A is travelling east at 15 m/s.

B is travelling north at 20 m/s.

At a certain instant both cars are 800 m from the intersection and approaching the intersection.



Find (i) the shortest distance between the cars

(ii) the distance each car is from the intersection when they are nearest to each other.

2008 – Higher Level – Question 2(a)

Two straight roads cross at right angles. A woman C, is walking towards the intersection with a uniform speed of 1.5 m/s.

Another woman D is moving towards the intersection with a uniform speed of 2 m/s.

C is 100 m away from the intersection as D passes the intersection.

Find (i) the velocity of C relative to D

(ii) the distance of C from the intersection when they are nearest together.

2009 – Higher Level – Question 2(b)

The speed of an aeroplane in still air is u km/h.

The aeroplane flies a straight line course from P to Q, where Q is north of P.

If there is no wind blowing the time for the journey from P to Q is T hours.

Find, in terms of u and T, the time to fly from P to Q if there is a wind blowing from the south-east with a speed of $4\sqrt{2}$ km/h.

2006 – Higher Level – Question 2(a)

Two aeroplanes A and B, moving horizontally, are travelling at 200 km/h relative to the ground. There is a wind blowing from the east at 60 km/h. The actual directions of flight A and B are north-west and north-east respectively.

- Find (i) the speed of aeroplane A in still air
 - (ii) the magnitude and direction of the velocity of A relative to B.

2008 – Higher Level – Question 2(b)

On a particular day the velocity of the wind, in terms of \vec{i} and \vec{j} , is $x\vec{i}-3\vec{j}$, where $x \in \mathbb{N}$.

 \vec{i} and \vec{j} are unit vectors in the directions East and North respectively.

To a man travelling due East the wind appears to come from a direction North α° West where $\tan \alpha = 2$.

When he travels due North at the same speed as before, the wind appears to come from a direction North β° West where $\tan \beta = \frac{3}{2}$.

Find the actual direction of the wind.

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2010 – Higher Level – Question 2(b)

When a motor-cyclist travels along a straight road from South to North at a constant speed of 12.5 ms^{-1} the wind appears to come from a direction North 45° East.

When she returns along the same road at the same constant speed, the wind appears to come from a direction South 45° East.

Find the magnitude and direction of the velocity of the wind.